

On an abstract nonlinear second order integrodifferential equation

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Abstract. The aim of the present paper is to study the global existence of solutions of nonlinear second order integrodifferential equation in Banach space. Our analysis is based on an application of the Leray-Schauder alternative and rely on a priori bounds of solutions..

1. Introduction

Let X be a Banach space with norm $\| \cdot \|$. Let $B = C([0, T], X)$ be the Banach space of all continuous functions from $[0, T]$ into X endowed with supremum norm

$$\|x\|_B = \sup \{ \|x(t)\| : t \in [0, T] \}.$$

The purpose of this paper is to prove the global existence of solutions of the following initial value problem for second order integrodifferential equations of the form

$$(1.1) \quad (r(t)x'(t))' = f \left(t, x(t), \int_0^t k(t, s)g(s, x(s))ds \right), \quad t \in [0, T]$$

$$(1.2) \quad x(0) = x_0, \quad x'(0) = 0;$$